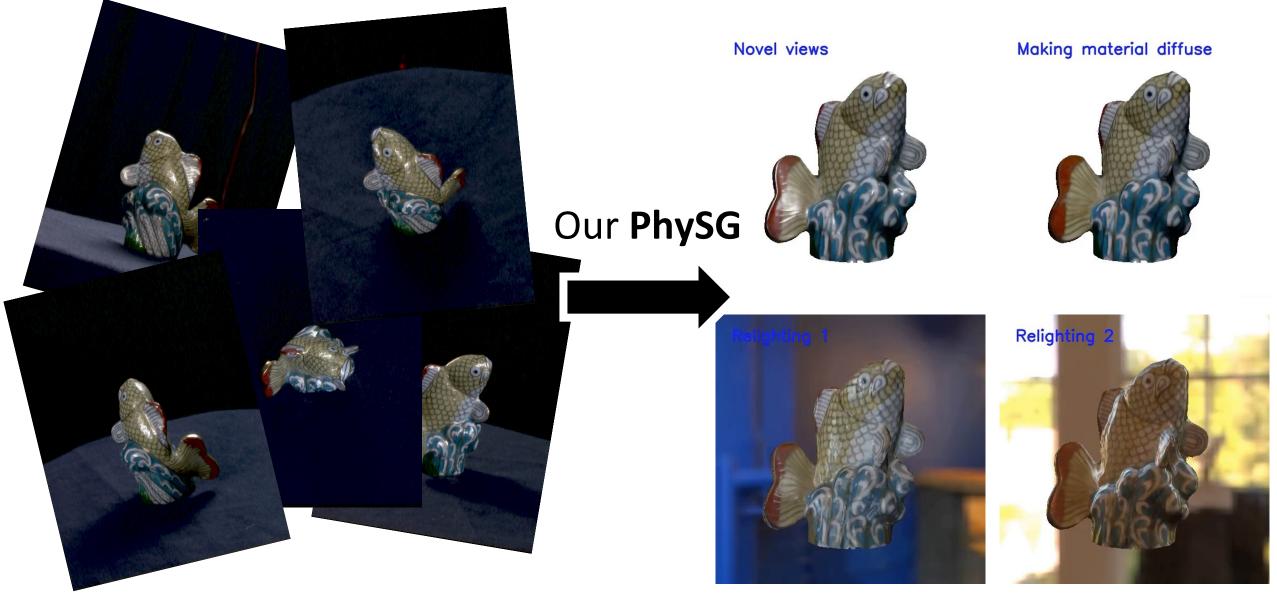


PhySG: Inverse Rendering with Spherical Gaussians for Physics-based Relighting and Material Editing Kai Zhang^{*}, Fujun Luan^{*}, Qiangian Wang, Kavita Bala, Noah Snavely (* equal contribution) **Cornell University**

Motivation: view synthesis + relighting + material editing



Our contribution: An efficient, differentiable framework for inverse rendering.

Assumptions: simplified rendering model.

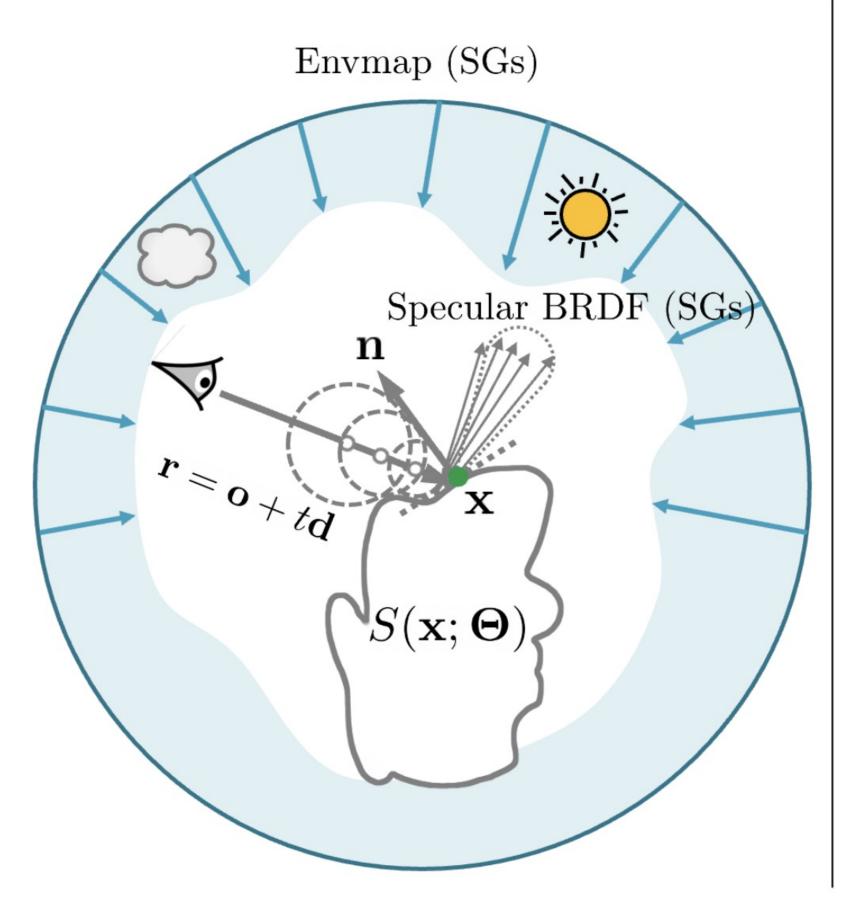
We start from the **rendering equation**:

$$L_o(\boldsymbol{\omega}_o; \mathbf{x}) = \int_{\Omega} L_i(\boldsymbol{\omega}_i) f_r(\boldsymbol{\omega}_o, \boldsymbol{\omega}_i; \mathbf{x}) (\boldsymbol{\omega}_i \cdot \mathbf{n}) \mathrm{d} \boldsymbol{\omega}_i$$

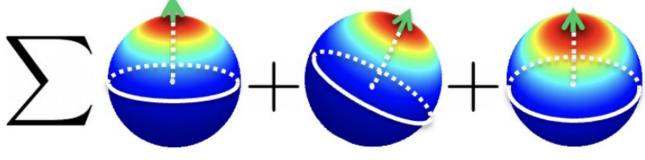
Approximate each term (lighting, material, cosine angle) with mixture of **spherical Gaussians** *G* in *closed-form*:

Incoming
light
$$L_{i}(\boldsymbol{\omega}_{i}) = \sum_{k=1}^{M} G(\boldsymbol{\omega}_{i}; \boldsymbol{\xi}_{k}, \lambda_{k}, \boldsymbol{\mu}_{k})$$
Surface
reflectance
$$f_{s}(\boldsymbol{\omega}_{o}, \boldsymbol{\omega}_{i}; \mathbf{x}) = G(\mathbf{h}; \mathbf{n}, \frac{\lambda}{4\mathbf{h} \cdot \boldsymbol{\omega}_{o}}, \mathcal{M}_{\mathbf{x}}\boldsymbol{\mu})$$
Cosine
term
$$\boldsymbol{\omega}_{i} \cdot \mathbf{n} \approx G(\boldsymbol{\omega}_{i}; 0.0315, \mathbf{n}, 32.7080) - 3$$

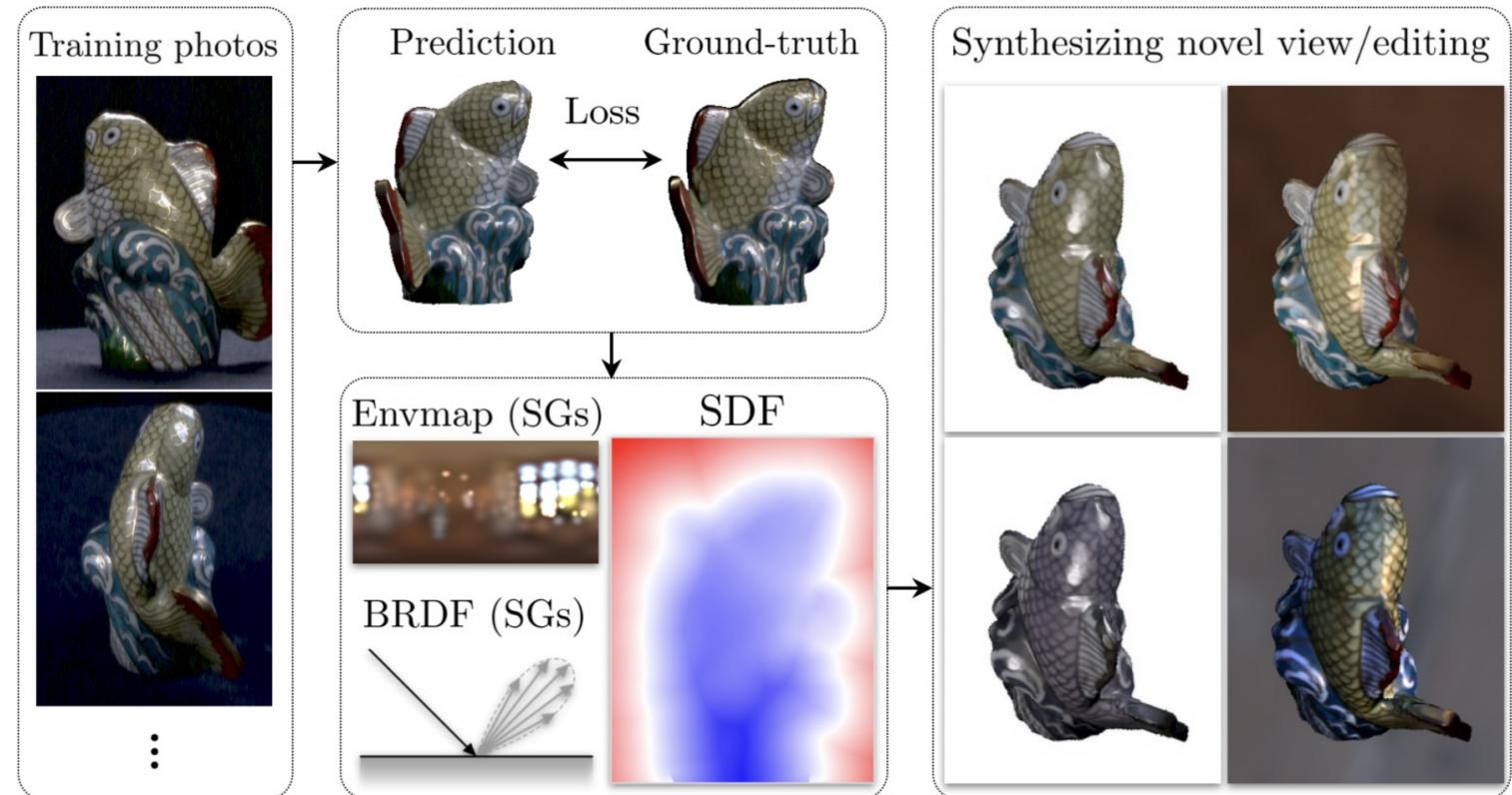
The **PhySG** rendering system:





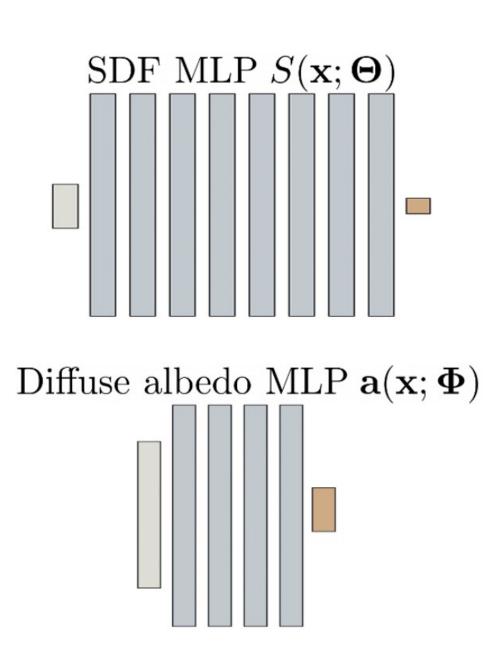


PhySG enables efficient end-to-end differentiable inverse rendering.

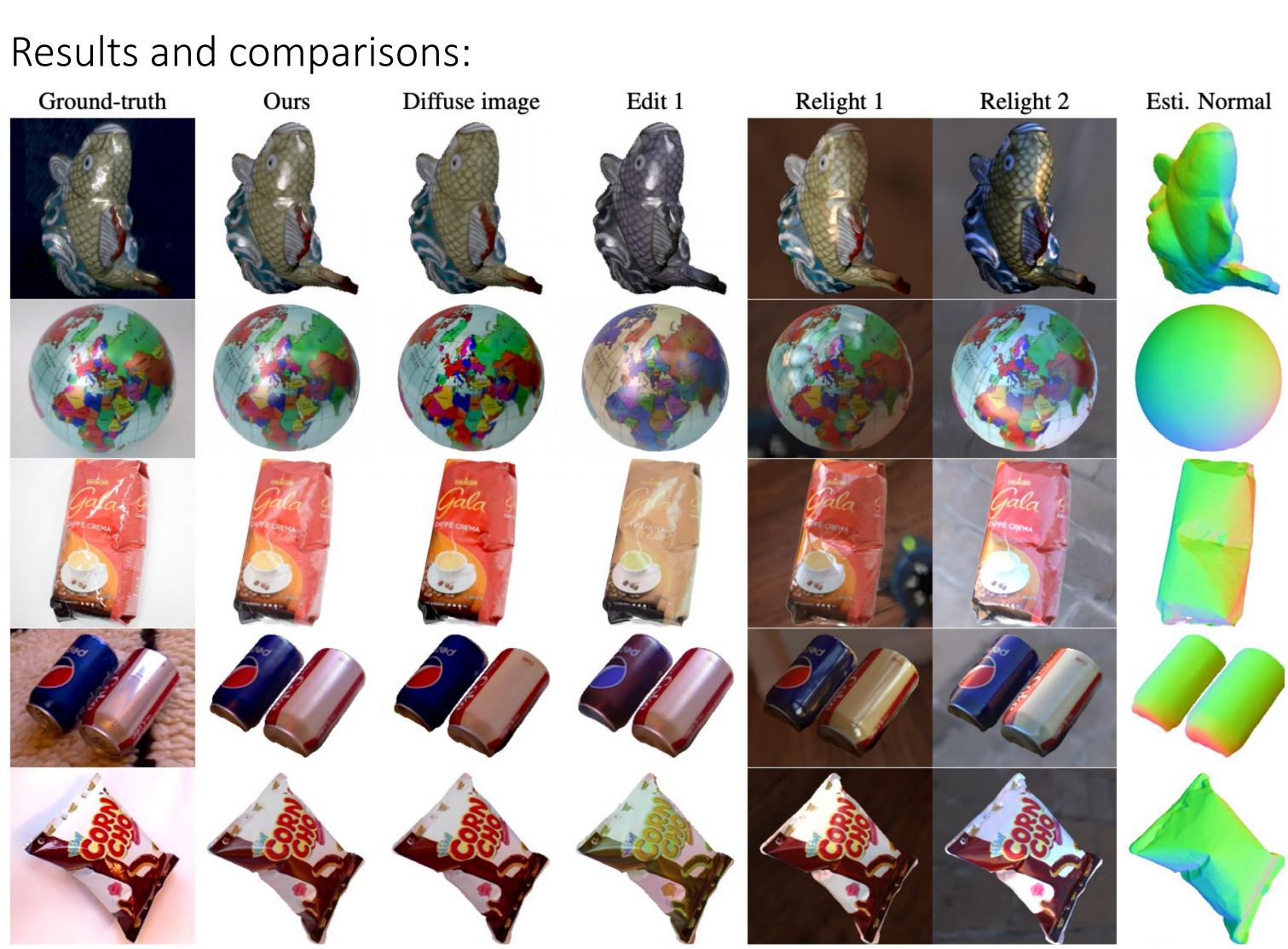


U)

31.7003



Specular BRDF f_s & Envmap L_i



Comparison of view extrapolation

| | ↓ LPIPS |
|-----------|---------|
| DVR | 0.1300 |
| NeRF | 0.0534 |
| IDR | 0.0188 |
| Our PhySG | 0.0170 |

Limitations:

- Specular BRDF is not spatially-varying
- Require object segmentation masks

Acknowledgements

This work was supported in part by the National Science Foundation (IIS-2008313, CHS-1900783, CHS-1930755).



Comparison of surface normal error

| • | ↓ Surface normal error (°) |
|-----------|-----------------------------------|
| DVR | 38.90 |
| NeRF | 36.05 |
| IDR | 2.207 |
| Our PhySG | 2.528 |

Lack modelling of self-occlusion and indirect illumination

Code available! *Project website:* tinyurl.com/PhySG-web

